

**From:** [Moody, Dustin \(Fed\)](#)  
**To:** (b) (6)  
**Subject:** Fw: Haven't heard from you in awhile. Are you good?  
**Date:** Thursday, April 11, 2019 3:08:35 PM

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**From:** Moody, Dustin (Fed)  
**Sent:** Thursday, April 11, 2019 2:45 PM  
**To:** Dang, Think H. (Fed)  
**Subject:** Re: Haven't heard from you in awhile. Are you good?

Think,

In Theorem 5, you were looking to find the new formula for the codomain curve where the formula holds with no  $w$  terms. I believe I've found them, and verified it by example.

The idea is just that you have the image of the point under the isogeny is:

$(XYZ : (2w+1) * \text{stuff} : (2w+1) * \text{stuff})$

You can compose with the isomorphism  $(x,y,z) \rightarrow (kx, ky, kz)$ .

So we use  $k=1/(2w+1)$ .

You then have something of the form  $(1/(2w+1)XYZ : \text{stuff} : \text{stuff})$ .

Then compose with the isomorphism  $(x,y,z) \rightarrow (kx,y,z)$ . This maps  $H_{\{a,d\}}$  to  $H_{\{ak^3,kd\}}$ .

This moves it to something of the form  $(XYZ : \text{stuff} : \text{stuff})$  with no  $w$ . That is, it's the same formula as in Theorem 5, but with no terms involving  $w$ .

The new image curve is  $H_{\{Ak^3,Dk\}}$ , where  $A,D$  are as you give in theorem 5, and  $k=1/(2w+1)$ .

Concretely, the image curve is

$$\text{newA} = -3(d^2c + 3dc^2 + 9a)/(2w+1)^2$$

$$\text{newD} = -3(d+6c)/(2w+1)^2$$

But then, note  $(2w+1)^2 = -3$ . So then

$$\text{newA} = d^2c + 3dc^2 + 9a$$

$$\text{newD} = d + 6c$$

And note also there is no problem in characteristic 3 now.

Dustin

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**From:** Moody, Dustin (Fed)  
**Sent:** Monday, April 8, 2019 1:35 PM  
**To:** Dang, Think H. (Fed)  
**Subject:** RE: Haven't heard from you in awhile. Are you good?

Think,  
We should meet again, and check our progress.

Dustin

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**From:** Dang, Think H. (Fed)  
**Sent:** Friday, April 5, 2019 1:15 PM  
**To:** Moody, Dustin (Fed) <dustin.moody@nist.gov>  
**Subject:** Re: Haven't heard from you in awhile. Are you good?

Hello Dr. Moody;

I've been working on the computational cost section.

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**From:** Moody, Dustin (Fed)  
**Sent:** Wednesday, April 3, 2019 10:22 AM  
**To:** Dang, Think H. (Fed)  
**Subject:** RE: Haven't heard from you in awhile. Are you good?

Any progress on the Hessian paper?

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**From:** Dang, Think H. (Fed)  
**Sent:** Thursday, March 28, 2019 1:32 PM  
**To:** Moody, Dustin (Fed) <[dustin.moody@nist.gov](mailto:dustin.moody@nist.gov)>  
**Subject:** Re: Haven't heard from you in awhile. Are you good?

Hello Dr. Moody;

I've been busy the last two weeks. I'm good.

Thank you.

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**From:** Moody, Dustin (Fed)  
**Sent:** Thursday, March 21, 2019 8:21 AM  
**To:** Dang, Think H. (Fed)  
**Subject:** Haven't heard from you in awhile. Are you good?

